5 In the diagram, $O$ is the centre of the circle. SAT and $B T$ are tangents to the circle. $A P$ is the diameter. $\angle S A C=58^{\circ}$ and $\angle A C B=50^{\circ}$.

(a) Show that triangle $A O T$ is congruent to triangle BOT.
(b) Find
(i) $\angle C A O, \square \square \square \square A \square \square \square O \square \square^{[1}$
(ii) $\angle A O B$,
(iii) $\angle B A O$,
(iv) $\angle A T B$,
(v) $\angle O B C$,
(vi) $\angle O P B$.

Show your working and give reasons.
(c) A point $D$ is such that $A C B D$ is a quadrilateral where $\angle A D B=130^{\circ}$.

Determine whether $D$ lies on the circumference of the circle.
$10 A, B, C$ and $D$ are four points on the circumference of a circle with centre $O . S T$ is a tangent to the circle at $B$. It is given that angle $A D B=50^{\circ}$ and angle $C B S=42^{\circ}$.
Calculate, showing your working clearly,

(a) angle $C O B$,

$$
\text { Answer Angle } C O B=\text {. }
$$

(b) angle $C D B$,

$$
\text { Answer Angle } C D B=
$$

(c) angle $A O C$.

21 (c) Explain how you can tell from the graph, the number of solutions to the equation $\frac{a}{x^{2}}=k$ for positive values of $k$.

Answer $\qquad$
$\qquad$
$\qquad$

22 The diagram shows a circle that passes through $A, B, C, D$ and $E$.
The lines $A E$ and $B D$ are parallel.
Angle $A D B=27^{\circ}$ and angle $A B E=49^{\circ}$.

(a) Find the angle $A F E$.

Show your working and give reasons.

4 (a) The cash price of a new washer-dryer is $\$ 2595$. It is also available on hire purchase with a deposit of one quarter of the cash price followed by monthly instalments of $\$ 60$ for three years.

Pavithra buys this washer-dryer on hire purchase.
(i) Calculate the rate of simple interest charged per annum, correct to two decimal places.
(ii) Find the extra cost of buying the washer-dryer on hire purchase as a percentage of the cash price.
(b) A sum of money grows to $\$ 5800.15$ in 3 years at a compound interest of $2.75 \%$ per annum. Find the sum of money if the interest is compounded quarterly.

5


The diagram shows a circle $Q R S T$, centre $O . U$ is the point of intersection of $Q S$ and diameter $R T$. $P Q$ and $P S$ are tangents to the circle such that angle $Q P S=40^{\circ}$. Angle $O S R=21^{\circ}$.

Find, with clearly stated reasons,
(a) obtuse angle $Q O S$,
(b) angle $Q T S$,
(c) angle $O S U$,
(d) angle $P Q T$.
$19 S, T, U, V$ and $W$ are points on a circle. $S V$ is the diameter and it intersects $T W$ at $X$. Angle $V T W=48^{\circ}$ and angle $T U V=127^{\circ}$.

(a) Find, stating your reasons clearly,
(i) angle $V S W$,

Answer
(ii) angle $T V S$,

Answer
(iii) angle $W X V$.

Answer
(b) Is $X$ the centre of the circle? Explain your answer, stating your reasons clearly.

Answer
$\qquad$
$\qquad$
$\qquad$
$\qquad$

13 The diagram shows a circle $A B C D$ with $B C=B D . C D E$ is a straight line. Given that angle $A B D=28^{\circ}$ and angle $A C B=25^{\circ}$,

(a) explain why is angle $A C D=28^{\circ}$.

## Answer

$\qquad$
$\qquad$
(b) Hence, find angle $B A D$, giving reasons for your answer.

